## Upper Elementary Geometry


(1)
atMONTESSORI

Volume of Figures Task Cards

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## Other Available ETC Montessori Geometry Materials

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1st Level Geometry Task Cards with Chart
2nd \& 3rd Level Geometry Task Cards
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Lower Elementary Attribute Work with Task Cards
Square Root Patterns

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Constructing 3D Compound Polyhedra
Constructing 3D Kepler-Poinsot Polyhedra
Constructing 3D Platonic Solids
Constructing 3D Pyramids
Constructing 3D Uniform Polyhedra
Geometry with Tangrams and Pattern Blocks
Deriving the Area of Geometric Figures
Understanding Geometric Constructions
Upper Elementary Attribute Task Cards
Upper Elementary Area Task Cards
Upper Elementary Volume Task Cards
Upper Elementary Geometry Task Cards

## Volume Answer Key

## Volume of a Rectangular Prism

| Card 1: | Varies | Varies | Varies |
| :---: | :---: | :---: | :---: |
|  | Volume | $\mathrm{V}=\mathrm{LxHxW}$ | Not Known |
| Card 2: | Varies | Varies | Varies |
|  | Volume | $\mathrm{V}=\mathrm{LxHxW}$ | Not Known |
| Card 3: | 12 ft | 8 ft | 26 ft |
|  | Volume | $\mathrm{V}=\mathrm{LxHxW}$ | Not Known |
| Card 4: | $6 \mathrm{in}^{2}$ | 12in | Not Known |
|  | Volume | $\mathrm{V}=\mathrm{LxHxW}$ | $32 \mathrm{in}{ }^{2}$ |
| Card 5: | 7ft. x 14ft | $7 \mathrm{ft} \times 6$ in | 6 in |
|  | Volume | $\mathrm{V}=\mathrm{LxHxW}$ | Not Known |


| Card 6: | 6in | 6in $\times 6$ in | Not Known |
| :--- | :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\mathrm{A}_{b} \mathrm{~h}$ | 12 in |

Card 7: $\quad 75 \mathrm{ft} \times 80 \mathrm{ft}$
$\frac{75 f t x 80 f t}{2}$
125ft

Volume

| Card 8: | $4 \mathrm{M} \times 16$ | $\mathrm{~V}=\mathrm{LxWxH}$ | 16 m |
| :--- | :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\mathrm{A}_{\mathrm{b}} \mathrm{h}$ | Not Known |
| Card 9: | $4.5 \mathrm{ft} \times 4.5 \mathrm{in}$ | 5in $\times 4.5 \mathrm{in}$ | 4.5 ft |
|  | Volume | $\mathrm{V}=\mathrm{A}_{\mathrm{b}} \mathrm{h}$ | Not Known |

## Volume of any Regular Prism:

| Card 1: | Not Known | $\frac{10 \times 8}{2}$ | 40 cm |
| :---: | :---: | :---: | :---: |
|  | Volume | Area of base x height | $\mathrm{V}=\mathrm{LxHxW}$ |
| Card 2: | Not Known | $\frac{160 \times 10}{2}$ | 50 cm |
|  | Volume | Area of base x height | $\frac{\text { base } \mathrm{x} \text { height }}{2}$ |
| Card 3: | Not Known | $96 \mathrm{ft}{ }^{2}$ | 4ft |
|  | Volume | Area of base x height | $\frac{P a}{2}$ |
| Card 4: | Not Known | $\frac{(B+b) h}{2}$ | $21 / 2$ |
|  | Volume of 2 Planter Boxes | Area of base x height | $\frac{b h}{2}$ |
| Card 5: | Not Known | $\frac{D d}{2}$ | $2^{1 / 2}$ |
|  | Volume | Area of base x height | $\frac{P a}{2}$ |
| Card 6: | $2.25 \mathrm{~cm}^{3}$ | $1.5 \mathrm{~cm}^{2}$ | Not Known |
|  | Height | $\mathrm{H}=\frac{V}{A b}$ | $=\frac{2.25 \mathrm{~cm}^{3}}{1.5 \mathrm{~cm}^{2}}$ |
| Card 7: | Not Known | $\frac{D d}{2}$ | 12ft |
|  | Volume | Area of base x height | LxWxH |


| Card 8: | 900,000 $\mathrm{yds}^{3}$ | $\frac{D d}{2}$ | Not Kn |
| :--- | :--- | :--- | :--- |
|  | Height | $\mathrm{H}=\frac{\text { Volume }}{\text { Area of base }}$ | Area of |
| Card 9: | Not Known | $112,500 \mathrm{ft}^{2}$ | 100 ft |
|  | Volume | $\mathrm{V}=\mathrm{A}_{\mathrm{b}}(\mathrm{H})$ | $\frac{b d}{2}$ |

## Volume of Pyramid:

| Card 1: | Not Known | $(120 \mathrm{ft} .)^{2}$ | 110ft |
| :---: | :---: | :---: | :---: |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | 210(110) |
| Card 2: | Not Known | $(14 \mathrm{~cm})^{2}$ | 8 cm |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | 5 cm |
| Card 3: | Not Known | $(2 \mathrm{ft})^{2}$ | 4ft |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | Dec. 25 |
| Card 4: | Not Known | $4 \mathrm{ft}^{2}$ | 8 ft |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $32 \mathrm{ft}^{2}$ |
| Card 5: | Not Known | $12 \mathrm{in}^{2}$ | 16 ft |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $192 \mathrm{in}^{2}$ |


| Card 6: | $1215 \mathrm{~cm}^{3}$ | $9 \mathrm{~cm}^{2}$ | Not Known |
| :--- | :--- | :--- | :--- |
|  | Height | $\mathrm{H}=\frac{3 V}{A b}$ | $\mathrm{~V}=\frac{(A b) h}{3}$ |
| Card 7: | Not Known | 225 cubits $^{2}$ | 35 cubits |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $225 \times 35$ |


| Card 8: | $1568 \mathrm{~cm}^{3}$ | Not Known | 8 cm |
| :--- | :--- | :--- | :--- |
|  | Area of base | $\mathrm{A}_{\mathrm{b}}=\frac{3 v}{h}$ | Volume |
| Card 9: | Not Known | $13 \mathrm{in} \times 22 \mathrm{in}$ | 36 in |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $2280 \mathrm{sq} . \mathrm{in}$. |

## Volume of an Oblique Square Pyramid

| Card 1: | Not Known | Ab |
| :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $\mathrm{~V}=\frac{(A b) h}{3}$


| Card 2: | $\mathrm{Ab}=\mathrm{S}^{2}$ | 27 blocks |
| :--- | :--- | :--- |
| Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $\mathrm{~V}=\frac{P a}{3}$ |


| Card 3: | Not Known | $\mathrm{Ab}=\mathrm{S}^{2}$ | 4Oft |
| :--- | :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $\mathrm{~V}=\frac{b h}{3}$ |
| Card 4: | $100 \mathrm{in}^{3}$ | Not Known | 12 in |
|  | Area of the Base | $\sqrt{a}=\frac{3(100)}{12}$ | $\mathrm{~V}=\frac{(A b) h}{3}$ |


| Card 5: | Not Known | $\mathrm{A}_{\mathrm{b}}=\mathrm{S}^{2}$ |
| :--- | :--- | :--- |
|  | $\mathrm{~V}=\frac{(A b) h}{3}$ |  |
|  | Volume | $V=\frac{s^{2}}{3}$ |


| Card 6: $1296 \mathrm{in}^{3}$ | $324 \mathrm{in}^{2}$ | Not Known |  |
| :--- | :--- | :--- | :--- |
|  | Height | $\frac{3(1296)}{324}$ | $\mathrm{~V}=\frac{(A b) h}{3}$ |
| Card 7: | $963333333.3 \mathrm{ft}^{3}$ | $\mathrm{~A}_{\mathrm{b}}(1700 \mathrm{ft})^{2}$ | Not Known |
|  | Height | $\mathrm{H}=\frac{3(V)}{A b}$ | 500ft |

$\left.\begin{array}{lll}\text { Card 8: } & \text { Not Known } & 3 \mathrm{~cm}^{2}\end{array}\right] 16 \mathrm{~cm}$.

Card 9: $6 \mathrm{in}^{3} \quad$ Not Known $\quad$ in Area of base and length of side base $\quad \mathrm{B}=\frac{3(V)}{h} \quad 5$

## Volume of a Cylinder

| Card 1: | Not Known | $\pi 6^{2}$ | 18 in |
| :--- | :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\mathrm{A}_{b} \mathrm{~h}$ | 12 |


| Card 2: | Not Known | $\pi\left(\frac{7}{2}\right)^{2}$ |
| :--- | :--- | :--- |
|  | $\mathrm{~V}=\mathrm{A}_{\mathrm{b}} \mathrm{h}$ | 15 |
|  | Volume | 7 |


| Card 3: | $13.5 \mathrm{in}^{3}$ | $\pi\left(\frac{3.5}{2}\right)^{2}$ |
| :--- | :--- | :--- | Not Known


| Card 4: | Not Known | $\pi 3^{2}$ |
| :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\mathrm{A}_{b} \mathrm{~h}$ |


| Card 5: | Not Known | $\pi\left(\frac{6}{2}\right)^{2}$ |
| :--- | :--- | :--- |
|  | $\mathrm{~V}=\mathrm{A}_{\mathrm{b}} \mathrm{h}$ | 8 cm |
|  | Volume | $6 \mathrm{~cm} \times 8 \mathrm{~cm}$ |


| Card 6: | Not Known | $\pi 6^{2}$ | 25 ft |
| :--- | :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\mathrm{A}_{\mathrm{b}} \mathrm{h}$ | $\mathrm{h}=\frac{V}{A b}$ |
| Card 7: | Not Known | $\pi 10^{2}$ | 12 cm |
|  | Volume | $\mathrm{V}=\mathrm{A}_{\mathrm{b}} \mathrm{h}$ | 20 cm |


| Card 8: | Not Known | $\pi 21^{2}$ | 16 in |
| :--- | :--- | :--- | :--- |
|  | Volume | $\mathrm{V}=\mathrm{A}_{b} \mathrm{~h}$ | 42 in |
| Card 9: | $942 \mathrm{~cm}^{3}$ | $\pi 5^{2}$ | Not Known |
|  | Height | $\mathrm{h}=\frac{V}{A b}$ | $\mathrm{~V}=\mathrm{A}_{b} \mathrm{~h}$ |

## Volume of a Sphere:

| Card 1: | Not Known | $\frac{6 c m}{2}$ | 3.15 |
| :---: | :---: | :---: | :---: |
|  | Volume | $\frac{4 \pi r^{3}}{3}$ | 18 cm |
| Card 2 : | Not Known | $\frac{2300}{2}$ | 3.14 |
|  | Volume | $\frac{4 \pi r^{3}}{3}$ | 12 |
| Card 3: | Not Known | 7 | 3.14 |
|  | Volume | $\frac{4 \pi r^{3}}{3}$ | 43.96 |
| Card 4: | Not Known | $\frac{4880}{2}$ | 3.14 |
|  | Volume | $\frac{4 \pi r^{3}}{3}$ | 15,330 km |
| Card 5: | Not Known | $\frac{150 f t}{2}$ | 3.14 |
|  | Volume | $\frac{4 \pi r^{3}}{3}$ | 75 ft |
| Card 6: | Not Known | 15 cm | 3.14 |
|  | Volume | $\frac{4 \pi r^{3}}{3}$ | 94.20 cm |
| Card 7: | Not Known | 6 cm | 3.14 |

Volume
$\begin{array}{lll}\text { Card 8: } & \text { Not Known } & \frac{1}{2} \frac{(56.52)}{3.14} \\ & \text { Volume } & \frac{4 \pi r^{3}}{3} \\ & & 3.14\end{array}$

| Card $9:$ | Not Known | 16 ft | 3.14 |
| :--- | :--- | :--- | :--- |
|  | Volume | $\frac{4 \pi r^{3}}{3}$ | $\pi r^{2}$ |

## Volume of a Cone:

| Card 1: | Not Known | $78.5 \mathrm{~cm}^{2}$ | 6 cm |
| :---: | :---: | :---: | :---: |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | 24 |
| Card 2: | Not Known | $\pi r^{2}$ | 10 cm |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | 31 |
| Card 3: | Not Known | $\pi 8^{2}$ | 6ft |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | 26 |
| Card 4: | Not Known | $\pi r^{2}$ | 12 cm |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $V=S^{3}$ |
| Card 5: | Not Known | Varies | Varies |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $\mathrm{V}=\frac{b h}{2}$ |
| Card 6: | $1105.28 \mathrm{~cm}^{3}$ | $50.24 \mathrm{~cm}^{2}$ | Not Known |
|  | Height | $\mathrm{h}=\frac{3 v}{b}$ | $\mathrm{V}=\frac{(A b) h}{3}$ |
| Card 7: | Not Known | $\pi r^{2}$ | 3ft |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $40 m^{2}$ |


| Card 8: | Not Known | 10 in |  |
| :--- | :--- | :--- | :--- |
|  | Area of base $\mathrm{in}^{3}$ | $\mathrm{~b}=\frac{3 v}{h}$ | $\mathrm{~V}=\frac{(A b) h}{3}$ |
| Card 9: | Not Known | $\pi \mathrm{r}^{2}$ | 12 cm |
|  | Volume | $\mathrm{V}=\frac{(A b) h}{3}$ | $\mathrm{~h}=\frac{A b}{b}$ |

## Surface Area of a Cylinder:

| Card 1: | Not Known | $\pi(1.25)^{2}$ | 4(2.5 $\quad$ ) |
| :---: | :---: | :---: | :---: |
|  | Surface Area | $\mathrm{AA}_{\text {circle }}+\mathrm{A}_{\text {rectangle }}$ | $2.5 \times 4$ |
| Card 2: | Not Known | $\pi\left(\frac{12}{2}\right)^{2}$ | 16(12r) |
|  | Surface Area | $\mathrm{AA}_{\text {circle }}+\mathrm{A}_{\text {rectangle }}$ | $16 \times 12$ |
| Card 3: | Not Known | $\pi\left(\frac{10}{2}\right)^{2}$ | 22(10 $)$ |
|  | Surface Area | $\mathbf{2 A}_{\text {circle }}+\mathrm{A}_{\text {rectangle }}$ | $10 \times 22$ |
| Card 4: | Not Known | $\pi\left(\frac{5}{2}\right)^{2}$ | $\frac{5 \pi(12)}{2}$ |
| Card 5: | Not Known | $\pi\left(\frac{4}{2}\right)^{2}$ | $\frac{4 \pi(8)}{2}$ |
|  | Surface Area | $\mathrm{SA}=\frac{\mathrm{lh}+\mathrm{Cr}}{2}$ | 4 in $x 8$ in |
| Card 6: | Not Known | $\pi\left(\frac{3.5}{2}\right)^{2}$ | $\frac{5 \pi(15)}{2}$ |
|  | Surface Area | $S A=\frac{1 \mathrm{~h}+\mathrm{Cr}}{2}$ | 3.5(15) |
| Card 7: | Not Known | 9 cm | $\frac{9}{2}$ |
|  | Surface Area | $4 \pi r^{2}$ | $9 \pi$ |

Card 8:
Not Known
6 cm
$\frac{6}{2}$
Surface Area $4 \pi r^{2}$ base
Card 9:
Not Known
40,000 km
$r=\frac{40,000}{2 \pi}$
Surface Area
$4 \pi r^{2}$
$\mathrm{b}=\frac{A}{h}$

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